

Cite this: *Digital Discovery*, 2024, 3, 355

# Machine learning interatomic potentials for amorphous zeolitic imidazolate frameworks†

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The detailed understanding of the microscopic structure of amorphous phases of metal–organic frameworks (MOFs) remains a widely open question: characterization of these systems is very difficult, both from the experimental and computational point of view. In molecular simulations, approaches have been proposed that rely either on reactive force field, that lack chemical accuracy, or first-principles calculations, that are too computationally expensive. Here, we have found an innovative solution to these problems by training a machine learning potential for the description of disordered phases of a zeolitic imidazolate framework (ZIF). We then used it to produce high-quality atomistic models of ZIF glasses, with accuracy close to density functional theory (DFT) but at far lower computational cost in production runs.

Received 5th December 2023  
Accepted 6th January 2024

DOI: 10.1039/d3dd00236e

rsc.li/digitaldiscovery

## Introduction

Metal–organic frameworks (MOFs) are a widely-studied class of nanoporous materials composed of metal nodes connected by organic linkers, exhibiting a wide range of applications including gas storage, catalysis, and drug delivery. While crystalline MOFs have been extensively studied and characterized, their amorphous counterparts have gained interest in the past decade.<sup>1</sup> However, the fundamental understanding of their structure at the microscopic level remains limited, and their physical and chemical properties are not well known. One key reason for the challenge lies in the inherent disorder and lack of long-range order in amorphous MOFs, which results in a complex and heterogeneous local environment.<sup>2</sup> Diffraction methods, which are widely used for the structural resolution of the crystalline phases, only offer indirect information about the structure of amorphous MOFs.<sup>3,4</sup>

Another factor is the intrinsically dynamic nature of amorphous MOFs, involving fluctuations in the coordination environment of metal nodes, conformational changes of organic linkers, and even guest molecule interactions. The lack of

a static, “perfect” structure makes it difficult to capture using simple models the fundamental nature of amorphous MOFs, and their structure–property relationships.<sup>5</sup> Overcoming these challenges requires the development of new experimental techniques and theoretical models to better probe the local atomic arrangements and dynamic processes within amorphous MOFs. Advances in this area are needed not only to deepen our understanding of these promising materials, but also pave the way for their rational design and optimization for applications.

Here, we turn our attention specifically to computational methods for the description of amorphous MOFs. While we refer the reader to ref. 6 for a full review, we can summarize the current state of the art by stating that four classes of methods have been used to build atomistic models of amorphous MOFs: (i) the application of inverse problem methods using constraints from available experimental data, in particular from X-ray or neutron-scattering experiments, in methods like Reverse Monte Carlo;<sup>7,8</sup> (ii) solving the same inverse problem with a physics-informed description of the interactions, for example in the polymatic approach;<sup>9,10</sup> (iii) mimicking the experimental melt-quench process *in silico*, through the use of *ab initio* molecular dynamics;<sup>11,12</sup> (iv) following the same process with reactive force fields, such as ReaxFF.<sup>13,14</sup>

Most of these methods rely on a description of the molecular interactions in the system. While the quality of this level of description is crucial to the validity of the models derived, none of the currently used options are truly satisfying. Classical force fields do not directly allow the description of bond breaking and formation. Reactive force fields are typically limited in the accuracy of their description of the chemical environment around metals,<sup>15</sup> leading to issues in the structures obtained

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† Electronic supplementary information (ESI) available: System description and methodological details for AIMD simulations, training of the MLPs and computation of mechanical properties. Volume, pressure and elastic constant convergence, *P*–*V* data, additional mechanical properties, radial distribution functions, potentials of mean force, angle distributions, porous volumes, ring statistics. See DOI: <https://doi.org/10.1039/d3dd00236e>



and their properties.<sup>16</sup> *Ab initio* methods have high chemical accuracy, but their expensive computational cost limits their use to small time and length scales, which in turn limits the statistical accuracy of the atomistic models obtained. In this work, we decided to apply a radically new approach to solve this issue by training a machine learning potential for the description of disordered phases of a zeolitic imidazolate framework (ZIF), and using it to produce high-quality atomistic models of ZIF glasses.

The use of machine learning potentials (MLPs) has emerged as a promising approach for describing interatomic interactions in both molecular systems and condensed matter.<sup>17–19</sup> MLPs leverage the power of machine learning algorithms to learn complex potential energy surfaces from a large amount of training data, enabling accurate and efficient modeling of interatomic forces. The use of MLPs bypasses the need for explicit functional forms or empirical parameterization typically used in traditional force fields, leading to more universal and adaptable models. A large diversity of MLPs are currently available and being developed, with contrasting features when it comes to their data requirements, computational cost in training and production, generalization ability, *etc.* In their most common use, MLPs are typically trained from large databases of atomic configurations and their associated energies and atomic forces, allowing the MLPs to encode complex relationships between atomic positions and the potential energy surface. This enables MLPs to accurately describe a wide range of phenomena, including bond breaking and formation, chemical reactions, and phase transitions – as long as the potential has been trained on representative data for these phenomena. Several studies have shown that MLPs are, in particular, well adapted for the description of amorphous phases of condensed matter – including multiple glass-forming materials – such as oxide glasses,<sup>20</sup> chalcogenide compounds,<sup>21</sup> silicates<sup>22</sup> or amorphous carbons.<sup>23</sup>

MLPs are trained on high-accuracy data that has been produced with computational chemistry methods of high computational cost, such as density functional theory (DFT) calculations, subsequently the trained MLP potential can rapidly evaluate interatomic forces and energies for arbitrary atomic configurations. There is therefore a large advantage in computational efficiency (several orders of magnitude) compared to the use of *ab initio* methods, while retaining an accuracy close to the reference level. This speed-up can allow for efficient exploration of complex systems, such as large-scale molecular dynamics simulations or high-throughput materials screening. In our case, it enables the simulations of amorphous ZIFs at time and length scales previously considered unreachable through first-principle calculations.

Despite the dramatic increase in the use of MLPs for both molecules and materials, only seven articles proposed MLPs for MOFs at the time of writing, all of them consisting of neural network potentials (NNP). MOFs are particularly challenging for multiple reasons, in particular because of the different interactions that need to be correctly modeled – from strong covalent bonds and ionic interactions to weak van der Waals interactions, along with their chemically complex composition. In

addition, the (often) large unit cell size impedes *ab initio* simulations from generating training data.<sup>24,25</sup> In 2019, Eckhoff and Behler<sup>24</sup> proposed the first MLP for a MOF system (MOF-5) and circumvented the need for large *ab initio* calculations by using DFT calculations of small molecular fragments to train their MLP for the periodic bulk framework. This method was applied on different systems in three later works in different groups.<sup>26–28</sup> However, the molecular fragments approach suffers from a lack of universal method to choose the fragments working on all MOFs, and from the sensitivity of its predicted energies to the choice of fragments. To overcome its shortcomings, four other works relied on periodic DFT calculations on the primitive cell of the framework to train their NNP.<sup>25,29–31</sup> An option proposed by Vandenhoute *et al.*<sup>29</sup> to solve the high computational cost of running *ab initio* simulations with large unit cells, was to use a data-efficient NNP (NequIP<sup>32</sup>) to reduce the number of *ab initio* calculations. Interestingly, this work also demonstrated that it was possible to simulate a phase transition for MOFs with MLPs, although the transition was non-displacive and did not involve any bond breaking. During the writing of this work, Goeminne *et al.* applied MLPs to describe the adsorption of CO<sub>2</sub> in two MOFs (ZIF-8 and Mg-MOF-74) to derive adsorption isotherms from first principles.<sup>33</sup>

Here, we use the case of the ZIF family of materials to show that machine learning potentials offer an attractive atomistic description of disordered phases of MOFs. Based on first-principles molecular dynamics, we trained neural network-based MLPs and used them to produce high-quality atomistic models of ZIF glasses, with accuracy close to density functional theory (DFT) but at much lower computational cost.

## Systems and methods

We provide here a brief summary of the system studied, and describe in detail the different computational methods used in this work. In order to make our work fully reproducible by others, representative input files for each type of simulation are available online in our data repository at <https://github.com/fxcoudert/citable-data> and the data set of configurations generated through *ab initio* MD and used for training and testing is made available on Zenodo at <https://doi.org/10.5281/zenodo.10015594>.

### ZIF-4

Our systems throughout this study belong to multiple phases of ZIF-4: the crystal, liquids, and multiple melt-quenched glasses.<sup>34</sup> The first amorphous MOF discovered and studied in detail,<sup>7</sup> ZIF-4 has since been the subject of numerous works and can be seen as a prototypical amorphous ZIF system.<sup>6</sup> It is built up from Zn<sup>2+</sup> metal nodes and imidazolate (Im) organic linkers, which are organized in the crystalline state as Zn(Im)<sub>4</sub> tetrahedra linked by Zn–N coordinative bonds as depicted in Fig. 1. There are several amorphous phases of this system,<sup>5</sup> which can be formed from the parent crystal by a variety of experimental methods, including ball milling, melt-quenching, or pressure-induced amorphization.<sup>2,35</sup> A representative model of a melt-



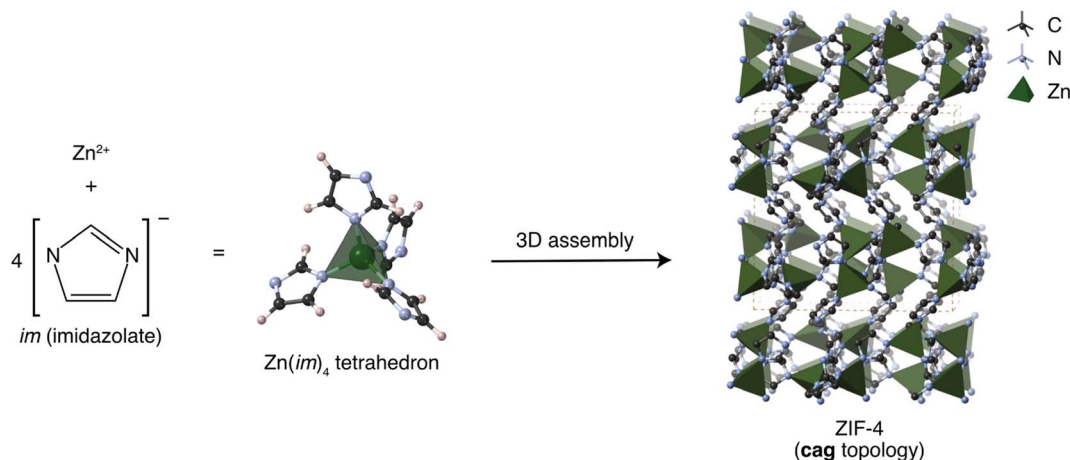


Fig. 1 Representation of the assembly of ZIF-4 as a three-dimensional network of  $\text{Zn}(\text{im})_4$  tetrahedra. Reproduced from ref. 6. Copyright 2022 American Chemical Society.

quenched glass of ZIF-4, gained from modelling synchrotron and neutron total scattering data, is presented in Fig. 2.

### Ab initio molecular dynamics

DFT-based MD simulations were performed following the protocol established in earlier work,<sup>16</sup> using the Quickstep module<sup>36</sup> of the CP2K software (version 6.1).<sup>37</sup> The exchange–correlation energy was evaluated in the PBE approximation,<sup>38</sup> and the dispersion interactions were treated at the DFT-D3 level.<sup>39</sup> Valence electrons were described by double- $\zeta$  valence polarized basis sets and norm-conserving Goedecker–Teter–Hutter pseudopotentials.<sup>40</sup>

The simulations were performed in the constant-volume ( $N, V, T$ ) ensemble with a fixed size and shape of the unit cell. A time step of 0.5 fs was used in the MD runs; the temperature was controlled by velocity rescaling<sup>41</sup> with a time constant of 1000 fs.

Reference data consisted in four trajectories of ZIF-4 liquids at four different volumes, and at temperatures of either 1500 K or 1750 K, all run for more than 50 ps. The preparation of these

systems is detailed in the ESI.† We also included a simulation of the ZIF-4 crystal at 300 K, for purposes of comparison.

### Flat histogram sampling

Flat histogram sampling is a powerful Monte Carlo approach used to overcome the limitations of traditional MC simulations, particularly when treating complex energy landscapes that feature rare events. Unlike standard simulations that rely on random sampling, flat histogram methods aim to ensure an equal exploration of all possible states or configurations within a system's phase space. For example, the Wang–Landau algorithm performs a non-Markovian random walk to build the density of states by quickly visiting all the available energy spectrum.<sup>42</sup> This resulting sampling distribution leads to a simulation where the energy barriers are invisible, meaning that the algorithm visits all accessible states (favorable and less favorable) much faster than a Metropolis algorithm. Flat histogram sampling has been applied to drive simulations to calculate density of states, explore the flexibility of nanoporous framework, and explore water adsorption.<sup>43–45</sup> We took inspiration from these approaches to develop sampling strategies to extract frames from the large amount of AIMD trajectories that represent the reference data.

The complete data set produced from AIMD trajectories features a total of 1 189 836 frames. We compared two approaches: random sampling and the flat-histogram approach. In the random sampling approach, configurations are taken at random from our very long AIMD trajectories, and then split randomly between training and test data. Due to the very large nature of our AIMD trajectories (four trajectories of more than 50 ps), the configurations available are widely spaced in time and there is no need to use specific methods to avoid correlation between configurations. In the flat-histogram approach, we first bin with respect to energy (with the number of bins corresponding to the requested number of samples), and then a random sample is taken from each bin. The resulting difference in energy distributions for the two different approaches is demonstrated in Fig. 3a. This process is

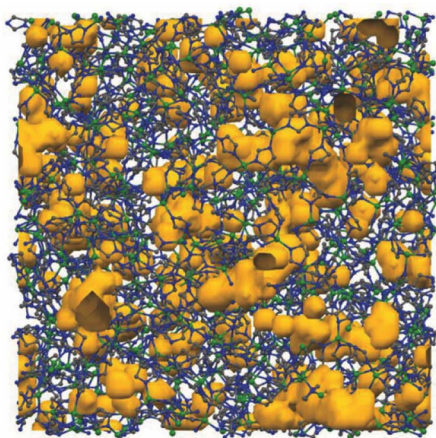


Fig. 2 Atomic configuration of the melt-quenched glass of ZIF-4. Reproduced from ref. 34.



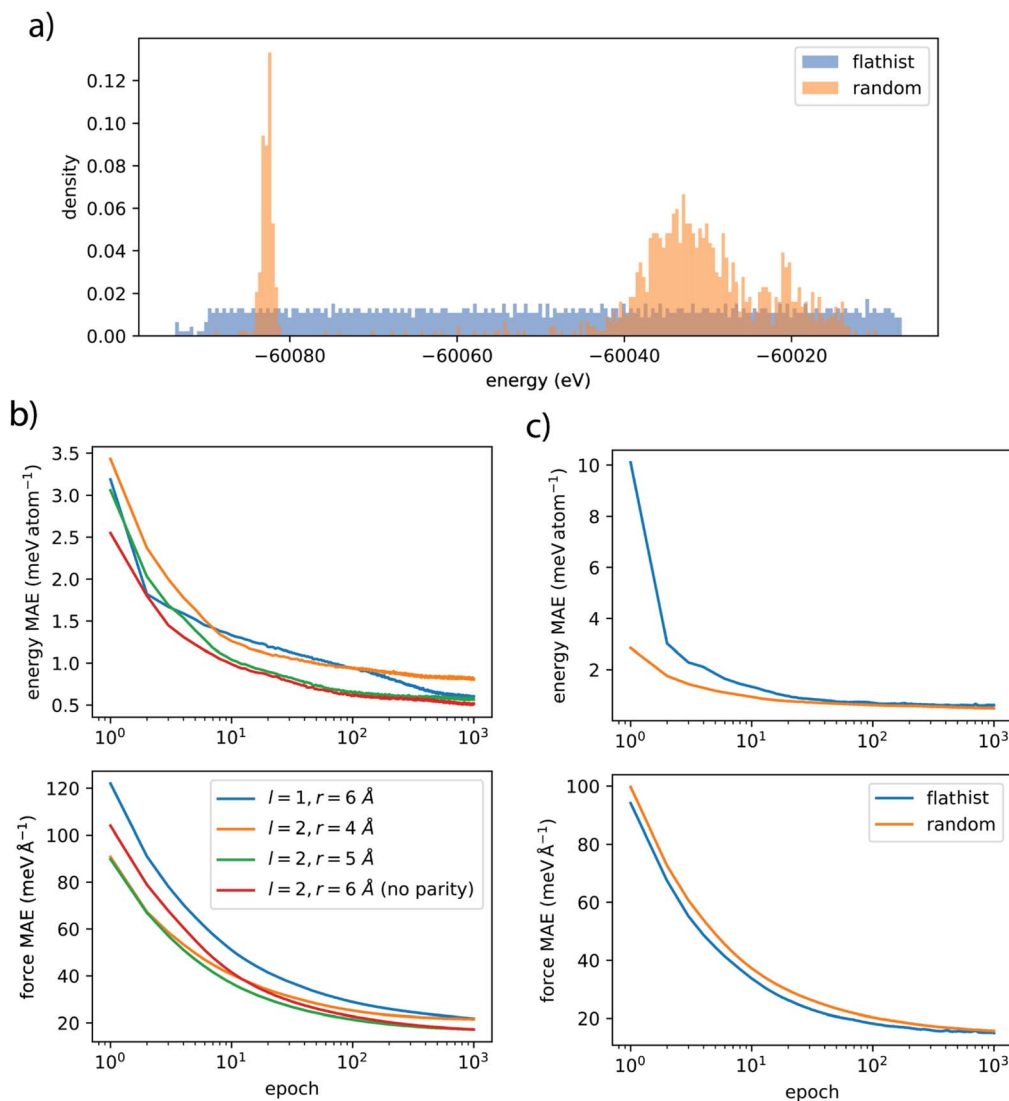


Fig. 3 (a) Comparison of the energy distributions of the initial data set with either random or flat-histogram (flathist) sampling. (b) Testing accuracy curves for energies and forces as a function of epochs, for difference values of hyperparameters on a random train-test data set. (c) Accuracy curves comparing the performance of random and flat-histogram sampling.

completed without replacement, and repeated, to give a 'training' data set and the leftover frames were subsequently sampled in the same way to give a 'test' set (data binning is repeated and unique for each data set). The unsampled frames were saved as 'validation'. An initial train-test data set was produced for both the random sampling approach for 1000 training samples and 100 test samples for hyperparameter screening, and a final train-test data set produced with the flat-histogram approach for 2500 training samples and 200 test samples. It is worth noting that, because of empty bins the flat-histogram approach at times produces less samples than bins; for examples the initial train-test data set was 964 and 96 samples and a final data set of 2357 and 190 samples.

### MLP architectures

NequIP (Neural Equivariant Interatomic Potential) is a recently published open-source code for building  $E(3)$ -equivariant

interatomic potentials,<sup>32</sup> building on the e3nn library.<sup>46</sup> It is a state-of-the-art message-passing neural network (MPNN)<sup>47</sup> framework that has been shown to produce high accuracy potentials with good training data efficiency,<sup>48</sup> due to its equivariance and because it directly operates on relative interatomic positions. It has demonstrated high accuracy across a wide variety of systems, including MOFs<sup>29</sup> and amorphous solids.<sup>32</sup>

As our goal is to produce large-scale models of amorphous systems, we also compared NequIP with Allegro, another approach of the same family and developed by the same group. The Allegro model is implemented as an extension of NequIP. It is a strictly local equivariant deep learning interatomic potential. Because it does not rely on atom-centered message passing, Allegro achieves much higher scalability in parallel (multi-GPU) computations, allowing the description of larger systems – up to 100 million atoms were demonstrated by its authors.<sup>49</sup>



## Choice of ML hyperparameters

The MLP models in this study were constructed using NequIP version 0.5.6 and Allegro (which does not have released version numbers). The models employed a cutoff radius chosen between 4 Å and 6 Å for the atomic environments and used five interaction layers. Feature representations were restricted to maximal rotation orders of either  $l = 1$  or  $l = 2$ , and for the largest cutoff radius (6 Å) features with odd mirror parity were neglected. The loss function consists of a weighted average of potential energy and force errors, and was optimized using the Adam algorithm and a learning rate of 0.005. We tested the choice of hyperparameters on the 1000–100 train-test data set with random sampling to determine the influence of rotation orders and cutoff radius. We also compared the choice of random or flat-histogram. This led us to choose a production model that used  $l = 2$  and a cut-off radius of 6 Å without parity as this enabled the highest accuracy with good efficiency. The production model was trained on the final flat-histogram dataset featuring 2357–190 samples.

For the Allegro model, we chose the same hyperparameters as for NequIP, in order to compare the accuracy and efficiency of the two models in a fair manner.

## MLP-based molecular dynamics

MD simulations with NequIP were performed using LAMMPS<sup>32,50</sup> with the pair\_nequip patch (available at [https://github.com/mir-group/pair\\_nequip](https://github.com/mir-group/pair_nequip)). By default, a time step of 0.5 fs was used in the MD runs, and was occasionally changed to 0.25 fs to simulate very high temperatures (above 1500 K). The temperature and pressure (when applicable) were controlled using a Nosé–Hoover thermostat and barostat. Temperature and pressure damping parameters were fixed at 100 fs and 1000 fs respectively. Several values around the chosen damping parameters were tested to check their relevance. Simulations were typically performed on a single unit cell for NequIP, and on a  $2 \times 2 \times 2$  supercell for Allegro.

A typical  $(N, V, T)$  simulation of a ZIF-4 unit cell (272 atoms) for 100 ps, required around 5 hours of computation on a single NVIDIA V100 GPU. It is a significant speedup compared to AIMD, for which 4 days and 160 CPUs (4 nodes of Intel Cascade Lake 6248) are required for the same system and duration.

## Structural properties

Structural analyses were performed using the Python library aMOF and the parameters detailed in a previous study.<sup>15</sup> aMOF is available online at <https://github.com/coudertlab/amof>, and the version used in this work is v1.1.0.

Unless explicitly stated in the figure caption, properties were averaged over an  $(N, V, T)$  trajectory of 100 ps for MLP simulations. Frames were taken every 100 fs for the radial distribution function (RDF), bond angle distribution and coordination number, every 500 fs for the mean square displacement (MSD), every 1 ps for ring statistics and every 10 ps for pore statistics. Reference *ab initio* properties were computed as in ref. 15.

The potential of mean force (PMF) was computed from the RDF  $g(r)$  through the relationship  $F(r) = -k_B T (\ln g(r) - \ln g_{\max})$ , where  $g_{\max}$  is the maximum of  $g(r)$  over  $r$ . The N–Zn–N angle distribution and Zn–N coordination numbers are computed by taking a cutoff radius of 2.5 Å for Zn–N distances, a value determined based on the Zn–N PMF, and validated in previous *ab initio*<sup>11,12,34</sup> and ReaxFF<sup>15</sup> studies. The total pore volume is computed on individual frames using the Zeo++ software,<sup>51–53</sup> as the sum of accessible and non-accessible volume with a helium probe of radius 1.2 Å.

Ring statistics were computed using the R.I.N.G.S. code<sup>54</sup> on the Zn–Im periodic graph obtained after identification of the building units. The definition of rings used in this work corresponds to the definition of “primitive rings” in the R.I.N.G.S. code (see ref. 15 for an extended definition). We used a maximum search depth of 32, safely above the largest rings of the ZIF-4 crystal.<sup>16</sup>

## Mechanical properties

Computation of finite temperature mechanical properties were performed as detailed in our recent study.<sup>16</sup> Two approaches were used in this work: the finite strain difference approach and the strain-fluctuation method. We focused on the example of the bulk modulus  $K$ , defined as  $K = -V(\partial P/\partial V)_T$ . Values of  $K$  reported in this work correspond to the equilibrium volume.

The finite strain difference approach consists in first establishing the  $P$ – $V$  relationship, and then fitting it with an equation of state (EoS).  $P$ – $V$  data is generated here by running multiple MD simulations in the  $(N, V, T)$  ensemble by enforcing the volume  $V$ , with the resulting pressure  $P(V)$  of the equilibrated system being measured. The well-behaved region of the  $P$ – $V$  data was fitted with the second order Birch–Murnaghan EoS.<sup>55</sup>

Mechanical properties at a given temperature  $T$  can also be evaluated from the fluctuations of a system at equilibrium, simulated under a constant stress in the  $(N, \sigma, T)$  ensemble. The bulk modulus can be obtained directly from the fluctuations of the volume, and multiple mechanical properties – bulk modulus  $K$ , Young's modulus  $E$ , shear modulus  $G$ , and Poisson's ratio  $\nu$  – can be computed from the elastic stiffness tensor  $C$  obtained from the fluctuations of the unit cell matrix.<sup>56</sup> Their computation was performed using the ELATE code<sup>57</sup> interfaced with the Python library aMOF. Values reported here were obtained with the Hill averaging scheme.

## Results and discussion

### Training and accuracy

We find that each of the models rapidly learns the energy and force of these complicated molecular systems, with the learning curves reaching a plateau in most cases before or near 1000 epochs, as seen on Fig. 3. Using the smaller initial data set we find the best accuracy is afforded by the  $l = 2, r = 6$  Å model which is unsurprising as this is the model with the most features. The  $l = 1, r = 6$  Å model provides a greater error in forces similar to  $l = 2, r = 4$  Å but at very high efficiency. Models with  $l = 2, r = 5$  Å or  $r = 6$  Å without parity provide similar



accuracy to  $r = 6 \text{ \AA}$  with parity, but again with much better efficiency.

Furthermore, we see that sampling the data set with the flat histogram method does not appear to provide more accuracy when tested against a large random sample. However, as observed in the training curves (Fig. 3c), it does appear to learn marginally faster for forces, in our specific case. As a result of the initial training on the smaller data set, we trained a model with  $l = 2$ ,  $r = 6 \text{ \AA}$  without parity (denoted here as “nequip deployed”) on a large data set created by flat histogram sampling. This model achieves near DFT accuracy on energy and forces, as summarized in Table 1. We also trained a model with Allegro, for the purpose of comparison, and in order to be able to perform molecular simulations on much larger systems. As expected, we found out that the strictly local Allegro model has lower accuracy, with a mean average error (MAE) of 0.70 meV on energy per atom (compared to 0.60 for NequIP), and  $30.1 \text{ meV \AA}^{-1}$  on forces (compared to 15.0 for nequip). On the other hand, we will show later than it has great scalability, and it uses only a fraction of the memory that NequIP requires.

During our study, we tested several different loss functions to simultaneously minimize the errors on the energy ( $E$ ), forces ( $\{F_i\}$ ) and stress ( $\sigma$ ) of the system. We found that training MLPs on energy and forces only is sufficient to reproduce the mechanical properties with reasonable accuracy (see ESI†) as expected from the errors in stress computed, and that including stress in the optimization of the MLP typically does not improve the quality of the model (and sometimes degrades it with respect to errors on energy and force). While this is counter-intuitive, it may come from the fact that instantaneous stress tensors computed during the *ab initio* dynamics suffer from a higher relative noise than the energy and forces.

## Reproducing structural properties

**Evaluation on reference systems.** To evaluate the quality of the generated MLP beyond figures of accuracy, we investigated a number of structural properties of the system used for training, *i.e.* the liquid, and of the crystal. Structural properties were evaluated over 100 ps ( $N, V, T$ ) trajectories at 300 K for the crystal and 1500 K for the liquid. The liquid underwent a preliminary 100 ps at 1500 K to ensure melting before collecting statistics. Here, we compare the properties obtained

with what we consider as reference data, namely the AIMD simulations of the same systems produced in previous work.<sup>34</sup>

Fig. 4 shows three local properties: the partial Zn–N radial distribution functions (RDF) and potential of mean force (PMF), along with the N–Zn–N bond angle distribution. In every case, we note an excellent reproduction of the *ab initio* properties. The MLP accurately emulates the crystal properties, thus demonstrating excellent transferability on this system, although it was trained on a different state (the liquid). Additionally, no change in coordination nor ring statistics is observed for the crystal (see Table S5†), and the computed porous volumes are fairly similar for every phase (see Table S6†). These data point to an excellent reproduction of the structural properties of both the system they were trained on, and the crystal.

**Validation on *ab initio* glasses.** To further explore the transferability on our MLP, we deployed the same strategy, *i.e.* MD runs and computation of structural properties, for unseen ZIF-4 systems consisting in the 10 *ab initio* glasses generated by Gaillac *et al.*,<sup>12</sup> which still represent the most reliable atomistic description of ZIF-4 glasses published to date in the literature.<sup>6,15</sup> Ten ( $N, V, T$ ) MD simulations with the NequIP MLP were run at 300 K for 100 ps starting from the glass models. All reported structural properties were averaged over the ten glasses.

Their local properties are reported on Fig. S3,† and accurately reproduce every local *ab initio* property (RDF, PMF and angle distribution). Additionally, no change in coordination between every MLP and AIMD data was reported, with coordination numbers and ring statistics being identical. It provides strong evidence that our NequIP MLP can accurately model a variety of ZIF-4 phases.

**Generating aZIF-4 glass models.** We showed above that the MLP we have produced provides a very accurate description of the structures of ZIF-4 in the crystal, glass and liquid phase. In order to further test its robustness and stability, we wanted to check whether it could be used in a broad thermodynamic space, to simulate the melt-quench process and generate new glass models. We followed the methodology established for ReaxFF glasses in ref. 15: we generated glass models and then compared their properties to *ab initio* data to evaluate the applicability of the MLP for this task, for which no satisfactory microscopic model has been published to date.<sup>6</sup>

**Table 1** Accuracy of energy, force and stresses computed for 10 000 frames of held-out data and estimated efficiency (using a NVIDIA Tesla V100) of the models based on 300 calls with 6 used for warm-up. Models are trained on the smaller random data set unless stated, while the deployed models are trained on the larger flat histogram sampled data set

	Energy MAE (meV)	Force MAE (meV $\text{\AA}^{-1}$ )	Stress MAE (MPa)	Efficiency ( $\mu\text{s}$ per atom per call)
$l = 1, r = 6 \text{ \AA}$	0.70	20.5	352	240
$l = 2, r = 4 \text{ \AA}$	0.90	20.7	304	371
$l = 2, r = 5 \text{ \AA}$	0.70	16.3	320	369
$l = 2, r = 6 \text{ \AA}$ (no parity)	0.60	16.4	352	280
$l = 2, r = 6 \text{ \AA}$	0.58	15.2	361	452
$l = 2, r = 6 \text{ \AA}$ (flat histogram)	0.61	17.8	360	453
NequIP deployed	0.60	15.0	352	282
Allegro deployed	0.70	30.1	352	347



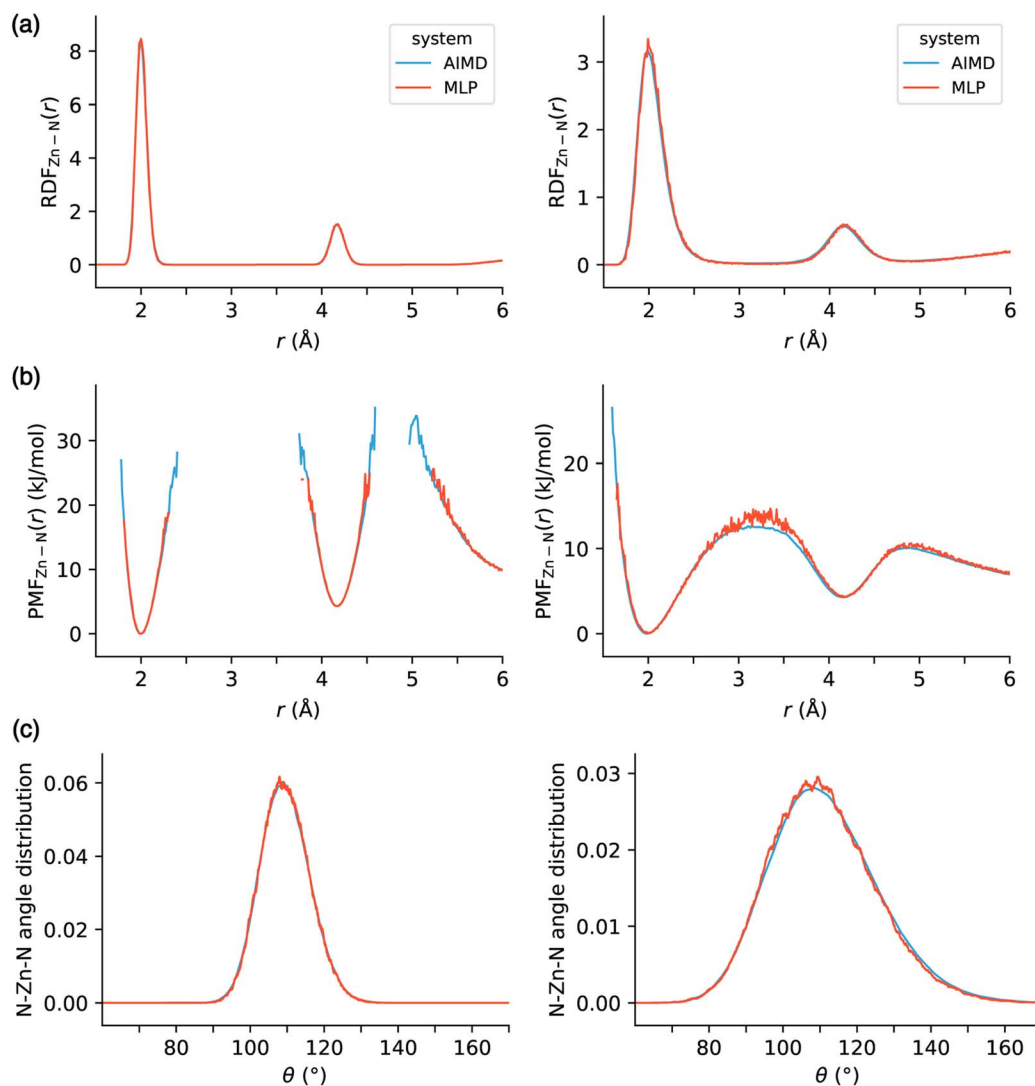


Fig. 4 (a) Radial distribution functions (RDF), (b) potentials of mean force (PMF) for the Zn–N atom pairs, and (c) distribution of the N–Zn–N angle for the ZIF-4 crystal (left) and liquid (right) with the NequIP MLP compared to AIMD.

**Melt-quenching.** Starting from the crystalline structure equilibrated at 300 K, the system was first melted to 1500 K, then quenched to room temperature, leading to the creation of a glassy state. The system was finally equilibrated for 100 ps, during which the calculation of the glass properties is performed. The four steps of this procedure are represented on Fig. 5. The entire procedure was performed in the  $(N, V, T)$  ensemble. To reduce finite size effects, a  $(2 \times 2 \times 2)$  supercell of ZIF-4 with 2176 atoms was simulated, with periodic boundary conditions. We checked that the use of a supercell led to a slight change in the properties of the generated glasses, compared to only simulating one unit cell (see details on Fig. S7†).

Melt-quenching is mainly parameterized by the maximal temperature  $T_{\max}$  and the heating/cooling rate  $r$ . Consistently with the previous *ab initio* work,<sup>12</sup> we aimed for a maximal temperature of 1500 K, and chose a rate of  $20 \text{ K ps}^{-1}$ .

Contrary to ReaxFF simulations which led to excessive decoordination, we find that ZIF-4 in simulations with the MLP

does not melt that easily. After a procedure consisting of only two ramps (one for heating, one for cooling), as with ReaxFF, the final system was still crystalline for  $T_{\max} = 1500 \text{ K}$  and  $r$  in the  $50\text{--}2.5 \text{ K ps}^{-1}$  region. Either lowering the rate to  $r = 1 \text{ K ps}^{-1}$ , or increasing the temperature to  $T_{\max} = 1900 \text{ K}$ , both led to the successful formation of glasses. However, the first option requires rather long simulations, while the second leads to an increased risk of loss of physical integrity.

Even if no breaking of the imidazolite rings was observed for  $1500 \text{ K} \leq T \leq 1900 \text{ K}$ , we chose a safer third option which consisted in keeping  $T_{\max} = 1500 \text{ K}$  and spending more time at the maximal temperature. A plateau of 50 ps at  $T_{\max}$  was enough to ensure melting, and therefore obtain a glass as highlighted on Fig. S4.†

**Properties of the glass models.** We first investigated the local order by examining the Zn–N bonds, comparing it to the *ab initio* crystal and glasses: On Fig. 6 and S5† we plot the partial RDFs for Zn–N and Zn–Zn, which highlight a remarkable



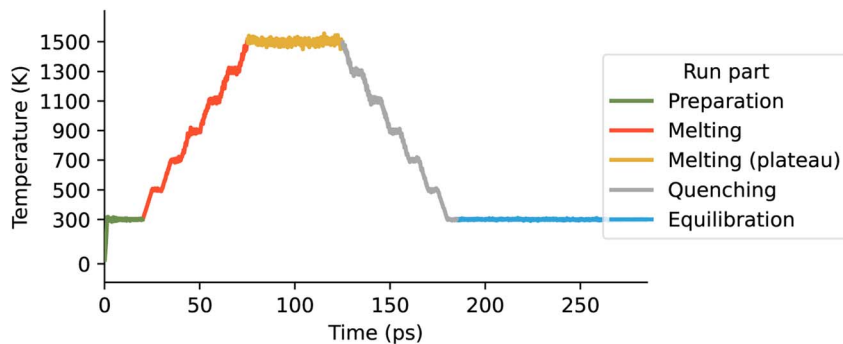


Fig. 5 Temperature as a function of time during the glass formation procedure, consisting of preparation (green), melting (red and orange), quenching (grey) and equilibration (blue). For clarity, a moving average over 25 fs is used.

agreement of the MLP glass with its *ab initio* counterpart. To contrast the differences in the region between the first two peaks, the Zn–N PMF is shown on the same figure. The PMF of the MLP glass resembles that of a glass, with the region between the first two peaks populated, with a similar profile to the *ab initio* glass apart from a slightly larger free energy barrier ( $\approx 26 \text{ kJ mol}^{-1}$ ).

We investigated the N–Zn–N angle distribution (plotted on Fig. 7a): the MLP glass demonstrates an excellent reproduction of the *ab initio* data, which is crucial because that property is key to the features of ZIFs, and is not well reproduced by other levels of description (such as ReaxFF). The angular PMF shown on Fig. 7b further confirms this accuracy, showing minimal deviations for angles away from the  $109.5^\circ$  of the  $\text{Zn}(\text{Im})_4$  tetrahedral structure. We then computed the porosity of the glasses

(see Fig. S6†) and found a total porous volume of  $61 \text{ cm}^3 \text{ kg}^{-1}$  for the MLP glass, comprised between the  $54 \text{ cm}^3 \text{ kg}^{-1}$  of the crystal and  $68 \text{ cm}^3 \text{ kg}^{-1}$  of the *ab initio* glass. This is in good agreement with the experimental measurements of the porosity of a ZIF-4 glass made by positron annihilation lifetime spectroscopy (PALS).<sup>58</sup>

Finally, we investigated the differences in the medium-range order of the glasses, by examining the coordination network built from the alternating Zn–Im units. We first calculated the average Zn–N coordination numbers and found a coordination of 3.93 for the MLP glass, the same value as the *ab initio* glass. We also computed Zn–Im ring statistics, to characterize the topology at a larger scale. Fig. 8 evidences that both glasses have topologies that deviate from the crystal's perfectly defined 8, 12

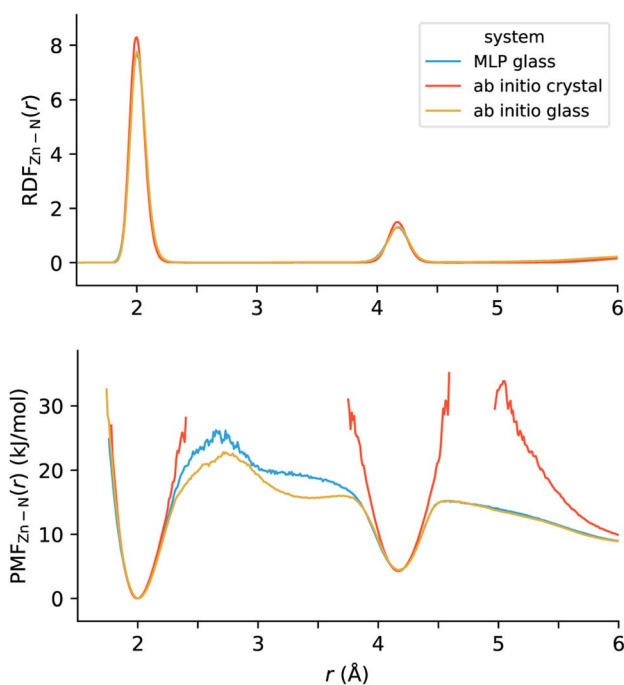


Fig. 6 Radial distribution function (RDF, top panel) and potential of mean force (PMF, bottom panel) for the Zn–N atom pairs of the MLP glass (blue), *ab initio* glass (orange) and *ab initio* crystal (red).

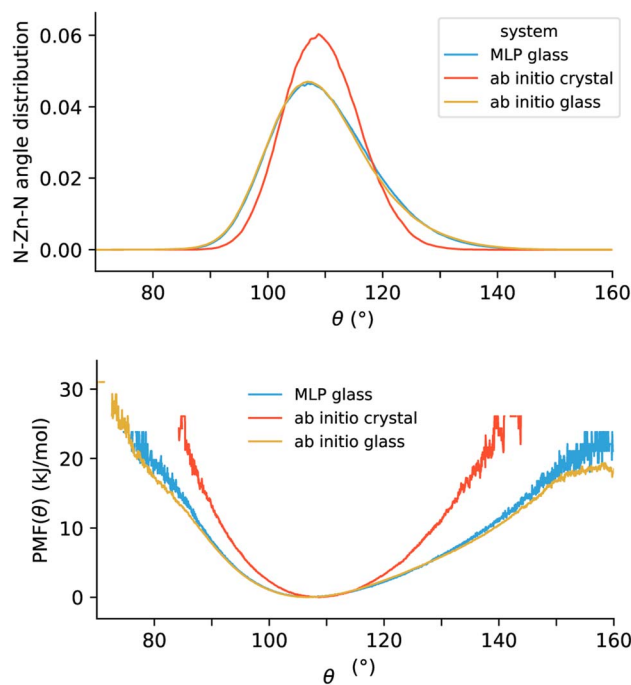


Fig. 7 Angular distribution (top panel) and potential of mean force (PMF, bottom panel) of the N–Zn–N angle for the MLP glass (blue), *ab initio* glass (orange) and *ab initio* crystal (red).





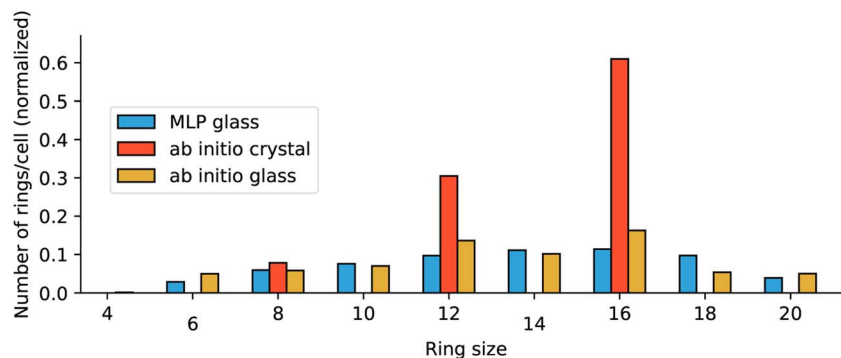


Fig. 8 Distributions of size of zinc-imidazolate alternate rings for the MLP glass (blue), *ab initio* glass (orange) and *ab initio* crystal (red).

and 16-membered rings. While not identical, the two glass models display rather similar topologies.

Overall, these elements show that the glass model generated with our MLP reproduces well many properties of the *ab initio* glasses, all the more when compared to how ReaxFF fares. Moreover, the MLP glass has characteristics in line with known experimental data,<sup>34</sup> providing strong evidence that aZIF models can be generated by MD simulations of melt-quenching with chemically accurate force fields.

### Mechanical properties

While the mechanical stability of MOFs is also essential to fully achieve their potential in industrial-scale processes, the study of how these materials respond to mechanical stress is comparatively still emerging.<sup>59,60</sup> While a series of experimental techniques have successfully been employed to determine the mechanical properties of crystalline MOFs, there is a lack of studies on the amorphous phases and very little data is available for now.<sup>35</sup> Computational methods offer an alternative method, but are rather expensive at the *ab initio* level,<sup>16</sup> which is why MLPs are of high interest in this context, being able to explore larger spatial and time scales. Several studies demonstrated how MLPs can be used to study various mechanical properties, including four applied to MOF materials.<sup>24,27,29,31</sup>

Here we focus on the bulk modulus ( $K$ ), a property that provides key information for applications, being related to MOF stability during the shaping process<sup>61</sup> or pressure swing adsorption (PSA) cycles.<sup>59</sup>

**Finite strain difference method.** To allow direct comparison to our AIMD reference results, we first compute  $K$  with the same method, namely the finite strain difference method. All simulations were performed in the  $(N, V, T)$  ensemble to enforce a volume  $V$  and compute the resulting pressure  $P(V)$  of the equilibrated system. The reduced computational cost allowed for smoother volumetric deformations (1.5% change over 100 ps) and a longer equilibration (100 ps, shown on Fig. S8†) than was possible with AIMD.

In order to offer a meaningful comparison, we considered several glass models: the same *ab initio* glass models studied with AIMD, and MLP glasses obtained by melt-quenching in the previous section. For consistency between *ab initio* and MLP

glasses, we used for both 10 single cell models and averaged results. These models are thoroughly presented in the ESI.† We checked that the use of a supercell did not seem to significantly impact the resulting bulk moduli  $K$  and density at zero pressure  $\rho_0$ , as exemplified on Table S7† in the case of the ZIF-4 crystal. The  $P$ - $V$  plot with the standard deviations as well as the fitted EoS is shown on Fig. S8† in the case of the crystal.

As shown on Table 2 and Fig. 9, we obtain a bulk modulus of  $K_{\text{crystal}} = 1.69$  GPa, in reasonable agreement with AIMD (1.39 GPa<sup>16</sup>) and previous experimental works – which found a value of 2.01 GPa with high-pressure crystallography<sup>62</sup> and 1.42 GPa with mercury intrusion.<sup>63</sup> Further interpretation is limited, as the precise value determined depends on the computational methodology and – for experiments – also on subtle differences between MOFs from different batches or on the experimental setup.<sup>62,64</sup> However, the comparison between two different systems within the same methodology is meaningful, and

Table 2 Bulk modulus  $K$  and density at zero pressure  $\rho_0$ , calculated with the finite strain difference method and MD simulations relying on the NequIP MLP, for three different systems: the ZIF-4 crystal, *ab initio* and MLP glass models

	Crystal	<i>Ab initio</i> glass	MLP glass
$K$ (GPa)	1.69	$3.43 \pm 1.23$	$3.24 \pm 0.72$
$\rho_0$ (g cm <sup>-3</sup> )	1.16	$1.25 \pm 0.06$	$1.29 \pm 0.04$

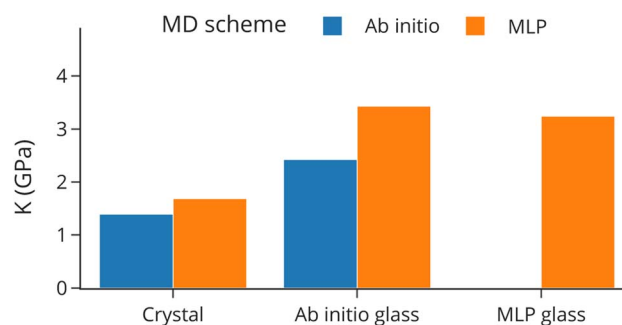


Fig. 9 Bulk modulus  $K$  for the ZIF-4 crystal and two glasses with the finite strain difference method with the NequIP MLP compared with AIMD.



calculations with the NequIP MLP reproduced the trend previously identified with other MD schemes, where glasses have larger  $K$  than the crystalline phase.

Interestingly, this finite strain difference approach also yields the density at zero pressure  $\rho_0$  which is of  $1.16 \text{ g cm}^{-3}$  for the crystal and of in the  $1.21$  to  $1.31 \text{ g cm}^{-3}$  range for the glasses. It is consistent with previous AIMD results<sup>46</sup> and experimental works<sup>65,66</sup> which showed that glasses have larger  $\rho_0$  than the crystalline phase. However, it should be noted that all densities are smaller than the experimental values of  $\rho_{\text{glass}} = 1.38 \text{ g cm}^{-3}$  (CO<sub>2</sub> physisorption study<sup>66</sup>) and  $\rho_{\text{crystal}} = 1.22 \text{ g cm}^{-3}$  (crystallographic density<sup>67</sup>).

**Strain-fluctuation method.** Another approach to obtain mechanical properties at a given temperature  $T$  is to evaluate them from the fluctuations of the unit cell in the constant-stress ( $N, \sigma, T$ ) ensemble.<sup>56</sup> Unlike the previous finite difference methods which only yield one property at a time, this leads to the estimation of the entire tensor of second-order elastic constants  $C$  which in turns is linked to mechanical properties such as Young's modulus, shear modulus, and Poisson's ratio.<sup>57</sup> This approach, already used for the ZIF-4 crystal with a classical force field,<sup>5,68</sup> requires long equilibration times ( $\sim 5$ – $10$  ns) and is out of reach of AIMD simulations, but proves tractable with MLPs. The bulk modulus can then also be computed from the fluctuations of the volume.<sup>56</sup> We also note that these very long simulations also highlight the good stability of the models trained as part of this work, which is a known issue for MLPs in some cases.<sup>69</sup>

Starting from the initial systems for the finite strain difference method, we performed further ( $N, P, T$ ) simulations with a flexible cell (LAMMPS keyword tri), corresponding to the ( $N, \sigma, T$ ) ensemble required by the method, until convergence of the volume (see Fig. S9†) and elastic constants (see Fig. S10†). From the results shown in Table S8,† we see that the values of  $K$  obtained from the elastic constants are consistent with the more robust volume fluctuations, as are the  $K$  and  $\rho_0$  values.

We summarize in Table 3 the mechanical properties we have calculated – Young's modulus  $E$ , shear modulus  $G$ , and Poisson's ratio  $\nu$  – some of which have never been reported for ZIF-4 glasses. In particular we reproduce the trend found in nano-indentation studies, with  $E$  being significantly larger in the glass than in the crystal (respectively  $8.2 \text{ GPa}$ <sup>65</sup> and  $4.6 \text{ GPa}$ ), although the values computed with this method are significantly smaller.

We conclude that MLPs are very powerful in the calculation of physical properties, such as mechanical properties, that are

typically very hard or impossible to compute at the DFT level of accuracy. Other physical quantities of interest, such as thermal properties, could be determined in the future from similar simulations.

### Producing larger glass models

**Accuracy of the allegro MLP.** We have seen already that MLPs based on *ab initio* data allow us to reach time and length scales not achievable previously at this level of accuracy. However, models trained with NequIP cannot be parallelized across multiple GPUs, and therefore are limited in the system size that can be achieved. In this last section, we have applied the very recent Allegro architecture,<sup>49</sup> which is based on NequIP but does not rely on message passing, and can therefore be parallelized across GPUs on a single compute node, as well as across multiple GPU nodes.

The training of our Allegro MLP has been described above already, as well as its accuracy on energies and atomic forces (see Table 1). The learning curves, and their comparison with NequIP, are presented in Fig. S11.† The main conclusion is that the MAE on forces for that Allegro model is twice as large as for NequIP, and we investigated the impact of this slightly lower accuracy on the physical properties of our systems. We found that the Allegro MLP reproduces very well the properties of low temperature systems (300 K): the ZIF-4 crystal and the *ab initio* glasses. As shown on Fig. 10, structural properties are reproduced as well as with NequIP when evaluated on 100 ps ( $N, V, T$ ) trajectories.

We also verified that Allegro can very efficiently simulate larger length scales, and found that that system sizes as large as a  $5 \times 5 \times 5$  supercell (containing  $\sim 34 \times 10^3$  atoms) can be computed easily. The local structural properties are – as expected – identical for different system sizes for a number of systems (see Fig. S17†) and therefore we report here results for ( $2 \times 2 \times 2$ ) supercells.

**Generation of glass models.** Simulating liquid formation using the Allegro MLP proved to be challenging. When examining the averaged structural properties of 1500 K ( $N, V, T$ ) trajectories, it appears that Allegro performs on par with NequIP as illustrated in Fig. S12.† However, upon closer investigation into the structural integrity with the help of our Python library aMOF, we identify broken imidazolate linkers. Such occurrences are relatively infrequent, typically happening once per single cell every 100 ps at 1500 K. By systematic checks, we found that every simulation above 1300 K could lead, if given enough time, to these unphysical events as shown in Fig. S14.† Temperatures below 1300 K, on the other hand, result in no organic bond breaking (see Fig. S13†).

We therefore adapted our procedure to produce glass models, by running a simulation at a sufficiently high temperature to observe structural rearrangement while keeping the simulation duration short enough to avoid the unphysical events. We carried an MD melt-quenching simulation with a maximal temperature ( $T_{\text{max}}$ ) of 1400 K, maintaining the simulation at this temperature for 100 ps: we observed melting while witnessing no imidazolate breaking during the process.

**Table 3** Mechanical properties for the ZIF-4 crystal and *ab initio* glasses obtained with the strain-fluctuation method and with the elastic stiffness tensor using the NequIP MLP

	Crystal	<i>Ab initio</i> glass
Bulk modulus $K$ (GPa)	1.58	$2.72 \pm 0.97$
Young's modulus $E$ (GPa)	2.49	$2.93 \pm 0.78$
Shear modulus $G$ (GPa)	1.01	$1.12 \pm 0.29$
Poisson's ratio $\nu$ (dimensionless)	0.24	$0.31 \pm 0.04$



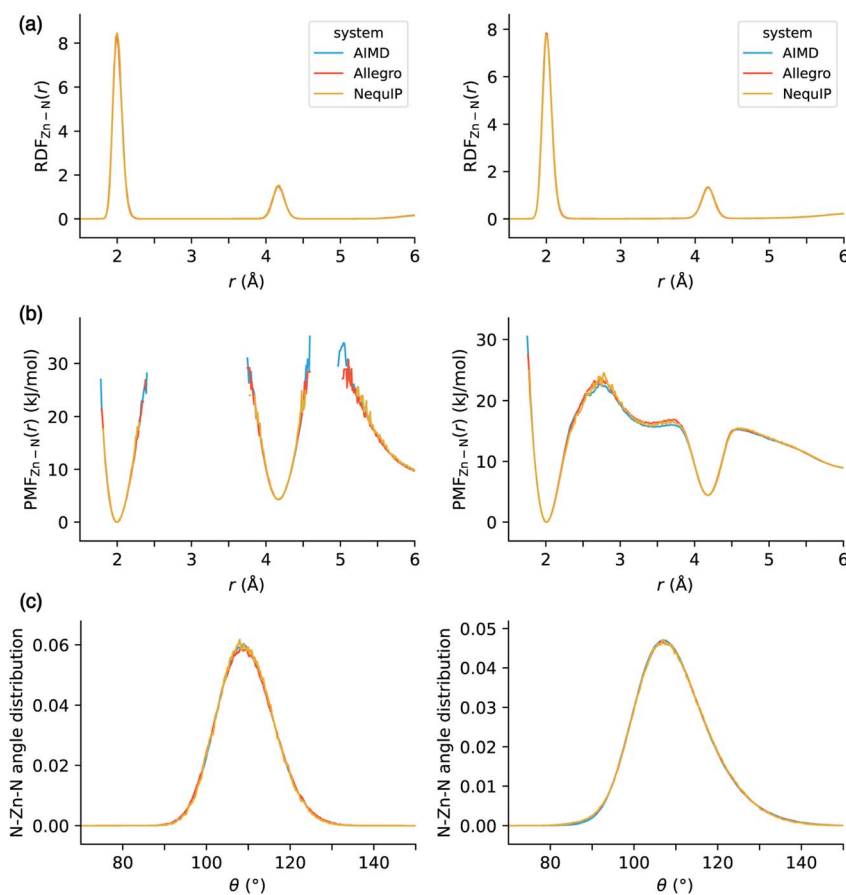


Fig. 10 (a) Radial distribution functions (RDF), (b) potentials of mean force (PMF) for the Zn–N atom pairs, and (c) distribution of the N–Zn–N angle for the ZIF-4 crystal (left) and *ab initio* glasses (right) with Allegro MLP compared to NequIP MLP and AIMD.

The final properties of the melt-quenched glass obtained with the Allegro model closely resemble those generated by NequIP, as depicted in Fig. S15.† The generated glass structures are however not identical, possessing distinct ring statistics (see Fig. S16†), as is expected because of the larger length scales accessible to the system. This shows the power of Allegro MLPs for the description of amorphous phases, as well as the creation of large-scale atomistic models of these phases.

## Conclusions and perspectives

In this work, we provide strong evidence that the development of machine learning potentials can pave the way towards the generation of multiple amorphous MOF models and the study of their properties. Using a dataset consisting of *ab initio* trajectories of liquid ZIF-4, we trained MLPs that led to an exceptional reproduction of the structural properties of multiple phases – crystal, liquid and several glasses – of ZIF-4. By generating new aZIF-4 models by melt-quenching, we demonstrated the potential of these MLPs to generate disordered models of MOFs at a fraction of the computational cost of AIMD. These models reproduce very well the local structure, framework topology, and macroscopic physical properties (such as mechanical behaviour) of the amorphous MOFs. Modern

parallelized MLPs can even allow us to reach model sizes up ten of thousands of atoms at a modest computational cost.

We think this development is a great perspective in the field of computational studies of disordered and amorphous framework materials. Previously, the choice of approaches required us to choose between the chemical accuracy of the description of intermolecular interactions, and the time and length scales achievable. On the one hand, first-principle methods were accurate but very expensive, and therefore limited by the lack of sampling of the phase space explored, as well as restricted to relatively short dynamics. On the other hand, reactive force field-based approaches were often inaccurate in their depiction of the chemistry at play. The use of MLPs based on *ab initio* data offer us a new way to approach the problem, and accelerate our quest of understanding the physical and chemical properties of these systems, and their relationship to local structure.

## Data availability

Representative input files for each type of simulation are available online in our data repository at <https://github.com/fxcoudert/citable-data> and the data set of configurations generated through *ab initio* MD and used for training and



testing is made available on Zenodo at <https://doi.org/10.5281/zenodo.10015594>.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

We thank Kim Jelfs and Tom Bennett for many inspiring discussions on this topic. Access to high-performance computing platforms was provided by GENCI grant A0150807069. This work was funded under the Imperial College London – CNRS PhD joint programme. JDE is the recipient of an Australian Research Council Discovery Early Career Award (project number DE220100163) funded by the Australian Government. Phoenix HPC service at the University of Adelaide are thanked for providing high-performance computing resources. This research was supported by the Australian Government's National Collaborative Research Infrastructure Strategy (NCRIS), with access to computational resources provided by Pawsey Supercomputing Research Centre through the National Computational Merit Allocation Scheme.

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