

Hadron Structure in Electroweak Precision Measurements

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August 1, 2014

Abstract

Precision measurements offer important, low-energy tests of the Standard Model. The Q_{weak} and (proposed) MOLLER experiments at Jefferson Lab are two such measurements. Since the interpretation of the experimental results depends on the precision of the theory prediction, radiative corrections need to be properly accounted for. In this thesis we examine the γZ box correction to the weak charge of the proton. Previously poorly understood, by using phenomenological information to constrain the input structure functions, we determine this important correction at Q_{weak} kinematics to a precision more than twice that of the previous best estimate. The γZ box is also evaluated at energies relevant to the MOLLER experiment for the first time.

The constructed Adelaide-Jefferson Lab-Manitoba model structure functions may also be used to study other low-energy phenomena. The electromagnetic parametrisations of the cross sections are utilised in the context of the generalised Baldin sum rule to investigate the momentum transfer dependence of the electric and magnetic polarisabilities. Additionally, both the electromagnetic and interference structure functions' moments were calculated in order to determine the higher-twist contributions to the structure functions. These results serve to increase our understanding of the internal structure of the nucleon.

Statement of Originality

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Acknowledgements

Firstly, thank you to Tony Thomas and Ross Young. If the title of, ‘World’s Best Supervisors’ had been up for grabs, I’m not sure that it would be any longer. Your encouraging feedback, confidence and timely help have made the completion of this thesis not only possible, but rewarding. Thank you to Wally Melnitchouk who has acted like a third, de facto supervisor and whose ideas drove much of this work. Your friendliness and hospitality made visits to Jefferson Lab as comfortable as if I had actually been living there. I would also like to thank Peter Blunden for your efforts in the work presented here and for offering a next step. Thank you also to Fred Myhrer and Will Detmold for allowing me to come and visit.

To my officemates Manuel, Phiala and (more recently) Ryan, thank you for your friendship, for hang-out times and for being willing to help and offer advice even when you had plenty of your own work to do. Phi, your drive and energy are simply amazing. Manuel, your hard work and perseverance are inspiring. Ryan, one day I may actually be able to answer some of your questions. To Ben, if there had been another desk in the office you would have easily fitted in. Thanks for the chats, lunches and help with the formatting and write-up of this thesis. Daniel, Adrian and Alex what am I going to do in Manitoba without the excuse of a football tournament to have gelati?

Dad and Mum, thank you for your belief, unwavering support and for allowing me complete freedom in pursuing this path. Jason, Josiah and Becky, thank you for your company outside of university life and for providing an outlet to take my mind off things. To everyone at Westbourne Park Uniting Church, and especially to members of my (past and present) small group, thanks for hanging in there with me—I’m finally finished! John Blanksby, thank you for your prayers and for providing a listening ear when I needed it.

Finally, God, thank you. Your mercies have been new every morning and your faithfulness has indeed been great.

Contents

1	Introduction	1
2	The Standard Model and beyond	5
2.1	The Standard Model	5
2.2	Electroweak theory	6
2.3	Beyond the SM	9
3	Precision tests of the SM	17
3.1	Atomic parity violation	17
3.2	Parity-violating electron scattering	18
3.3	Radiative corrections to Q_W^p	20
3.4	The $\square_{\gamma Z}$ correction	22
4	Structure functions	27
4.1	Deep inelastic scattering	29
4.2	Quark-parton model	32
4.3	Modelling structure functions	33
4.4	γZ interference structure functions	38
5	Adelaide-Jefferson Lab-Manitoba model	43
5.1	Electromagnetic parametrisation	43
5.2	AJM γZ interference structure functions	48
5.3	Phenomenological constraints	50
6	The $\square_{\gamma Z}^V$ correction	65
6.1	γZ box corrections for Q_{weak}	66
6.2	Predictions for parity-violating asymmetries	69
6.3	Q_W^p at 11 GeV	72
6.4	A_{PVDIS} for the proton at 11 GeV	82
7	Electric and magnetic polarisabilities of the proton	85
7.1	The generalised Baldin sum rule	85
7.2	Q^2 dependence of α and β	88

8	Quark-hadron duality	95
8.1	Duality in the SM	95
8.2	Moments of structure functions	97
8.3	Implications for the $\square_{\gamma Z}^V$ correction	103
9	Summary and conclusion	105
A	Further determinations of $\Re \square_{\gamma Z}^V$	109
B	List of publications	111
	Bibliography	113